

GATE-2011

Question Paper

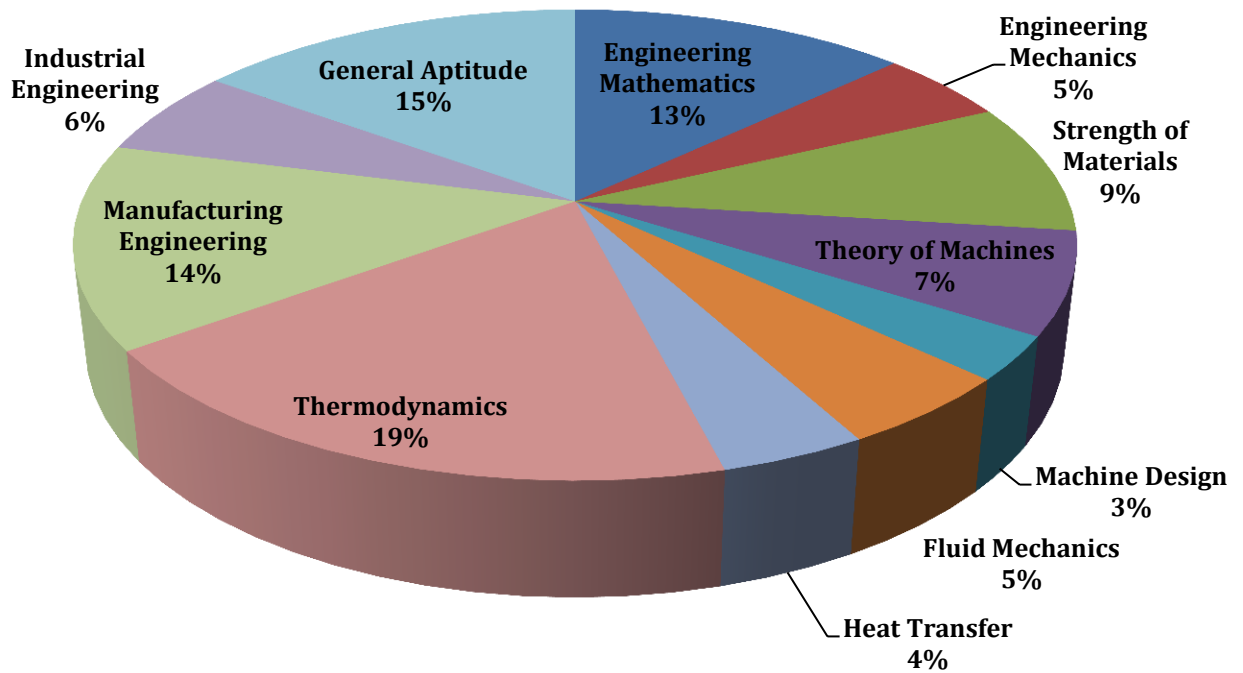
&

Answer Keys

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1. Question Paper Analysis
2. Question Paper & Answer keys

ANALYSIS OF GATE 2011 Mechanical Engineering



GATE-2011- ME

SUBJECT	NO OF QUESTION	Topics Asked in Paper	Total Marks
Engineering Mathematics	1M:5 2M:4	Calculus Complex Variables Linear Algebra Probability and Distribution Differential Equation Numerical Method	13
Engineering Mechanics	1M:1 2M:2	Kinematics & Dynamics of particles & rigid bodies in plane FBD & Equilibrium	5
Strength of Materials	1M:3 2M:3	Euler's Theory of Columns SFD & BMD Deflection of Beams Thick and Thin Cylinder Mohr's Circle	9
Theory of Machines	1M:1 2M:3	Mechanism Vibration	7
Machine Design	1M:1 2M:1	Failure Theories Design of shafts, gears & Bearings	3
Fluid Mechanics	1M:1 2M:2	Fluid properties Boundary Layer Fluid Kinematics	5
Heat Transfer	1M:2 2M:1	Heat Exchanger Conduction	4
Thermodynamics	1M:3 2M:8	Basic Thermodynamics Work, Heat & Entropy Power Engineering Psychrometrics I.C. Engines	19
Manufacturing Engineering	1M:6 2M:4	Joining Process Forming Process Metal casting Engineering Materials Metrology and Inspection Machining and Machine Tool Operation	14
Industrial Engineering	1M:2 2M:2	Production planning & control Operations Research	6
General Aptitude	1M:5 2M:5	Verbal Ability Numerical Ability	15
Total	65		100

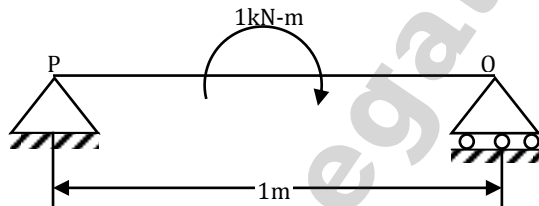
GATE 2011 Examination
MECHANICAL ENGINEERING

Q.1 to Q. 25 carry one marks each.

1. A streamline and an equipotential line in a flow field
 (A) Are parallel to each other (C) Intersect at an acute angle
 (B) Are perpendicular to each other (D) An identical
[Ans. B]
2. If a mass of moist air in an airtight vessel is heated to a higher temperature, then
 (A) specific humidity of the air increases (C) relative humidity of the air increases
 (B) specific humidity of the air decreases (D) relative humidity of the air decreases
[Ans. D]

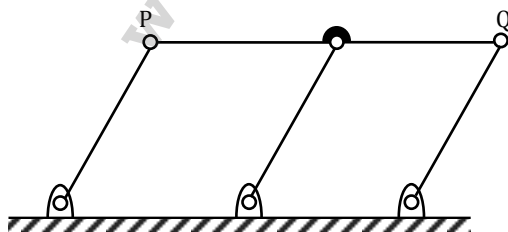
3. In a condenser of a power plant, the steam condenser at a temperature of 60°C . the cooling water enters at 30°C and leaves at 45°C . the logarithmic mean temperature difference (LMTD) of the condenser is
 (A) 16.2°C (C) 30°C
 (B) 21.6°C (D) 37.5°C
[Ans. B]

4. A simple supported beam PQ is loaded by a moment of 1 kN-m at the mid-span of the beam as shown in the figure. The reaction forces R_P and R_Q at supports P and Q respectively are



- (A) 1 kN downward, 1 kN upward (C) 0.5 kN downward, 0.5 kN upward
 (B) 0.5 kN upward, 0.5 kN downward (D) 1 kN upward, 1 kN downward
[Ans. A]

5. A double – parallelogram mechanism is shown in the figure. Note that PQ is a single link. The mobility of the mechanism is



- (A) -1 (C) 1
 (B) 0 (D) 2
[Ans. C]

6. The maximum possible draft in cold rolling of sheet increases with the
 (A) increase in coefficient of friction (C) decrease in roll radius
 (B) decrease in coefficient of friction (D) increase in roll velocity
[Ans. A]
7. The operation in which oil is permeated into the pores of a powder metallurgy product is known as
 (A) mixing (C) impregnation
 (B) sintering (D) infiltration
[Ans. C]
8. A hole is of dimension $\phi 9^{+0.015}$ mm. The corresponding shaft is of dimension $\phi 9^{+0.001}$ mm. The resulting assembly has
 (A) loose running fit (C) transition fit
 (B) close running fit (D) interference fit
[Ans. C]
9. Heat and work are
 (A) Intensive properties (C) Point functions
 (B) Extensive properties (D) Path functions
[Ans. D]
10. A column has a rectangular cross- section of 10 mm × 20 mm and a length of 1m. the slenderness ratio of the column is close to
 (A) 200 (B) 346 (C) 477 (D) 1000
[Ans. B]
11. A series expansion for the function $\sin \theta$ is
 (A) $1 - \frac{\theta^2}{2!} + \frac{\theta^4}{4!} - \dots$ (C) $1 + \theta + \frac{\theta^2}{2!} + \frac{\theta^3}{3!} + \dots$
 (B) $\theta - \frac{\theta^3}{3!} + \frac{\theta^5}{5!} - \dots$ (D) $\theta + \frac{\theta^3}{3!} + \frac{\theta^5}{5!} + \dots$
[Ans. B]
12. Green sand mould indicates that
 (A) polymeric mould has been cured (C) mould is green in colour
 (B) mould has been totally dried (D) mould contains moisture
[Ans. D]
13. What is $\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta}$ equal to?
 (A) θ (B) $\sin \theta$ (C) 0 (D) 1
[Ans. D]
14. Eigen values of a real symmetric matrix are always
 (A) Positive (C) Negative
 (B) Real (D) Complex
[Ans. B]

15. A pipe of 25 mm diameter carries steam. The heat transfer coefficient between the cylinder and surrounding is $5 \text{ W/m}^2\text{K}$. It is proposed to reduce the heat loss from the pipe by adding insulation having a thermal conductivity of 0.05 W/mK . Which one of the following statements are TRUE?
- (A) The outer radius of the pipe is equal to the critical radius.
 (B) The outer radius of the pipe is less than the critical radius.
 (C) Adding the insulation will reduce the heat loss.
 (D) Adding the insulation will increase the heat loss.

[Ans. C]

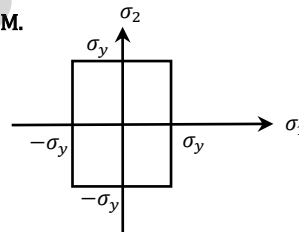
16. The contents of a well - insulated tank are heated by a resistor of 23Ω in which 10 A current is flowing. Consider the tank along with its contents as a thermodynamic system. The work done by the system and the heat transfer to the system are positive. The rates of heat (Q), work (W) and change in internal energy (ΔU) during the process in kW are
- (A) $Q = 0, W = -2.3, \Delta U = +2.3$ (C) $Q = -2.3, W = 0, \Delta U = -2.3$
 (B) $Q = +2.3, W = 0, \Delta U = +2.3$ (D) $Q = 0, W = +2.3, \Delta U = -2.3$

[Ans. A]

17. Match the following criteria of material failure, under biaxial stresses σ_1 and σ_2 and yield stress σ_y , with their corresponding graphic representations:

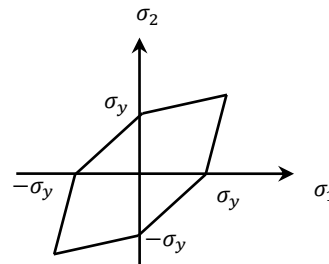
P. Maximum - normal - stress criterion

M.



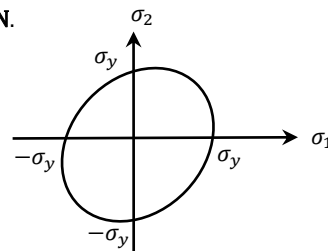
Q. Maximum - distortion - energy criterion

L.



R. Maximum - shear - stress criterion

N.



(A) P - M, Q - L, R - N

(C) P - M, Q - N, R - L

(B) P - N, Q - M, R - L

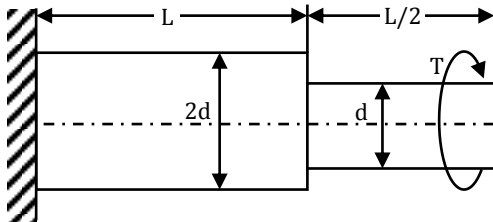
(D) P - N, Q - L, R - M

[Ans. C]

18. The product of two complex numbers $1 + i$ and $2 - 5i$ is
 (A) $7 - 3i$ (C) $-3 - 4i$
 (B) $3 - 4i$ (D) $7 + 3i$
[Ans. A]
19. Cars arrive at a service station according to Poisson's distribution with a mean rate of 5 per hour. The service time per car is exponential with a mean of 10 minutes. At steady state, the average waiting time in the queue is
 (A) 10 minutes (C) 25 minutes
 (B) 20 minutes (D) 50 minutes
[Ans. D]
20. The word **kanban** is most appropriately associated with
 (A) economic order quantity (C) capacity planning
 (B) just - in - time production (D) product design
[Ans. B]
21. If $f(x)$ is an even function and a is a positive real number, then $\int_{-a}^a f(x)dx$ equals
 (A) 0 (C) a
 (B) $2a$ (D) $2 \int_0^a f(x)dx$
[Ans. D]
22. The coefficient of restitution of a perfectly plastic impact is
 (A) 0 (C) 2
 (B) 1 (D) ∞
[Ans. A]
23. A thin cylinder of inner radius 500 mm and thickness 10 mm subjected to an internal pressure of 5 MPa. The average circumferential (hoop) stress in MPa is
 (A) 100 (C) 500
 (B) 250 (D) 1000
[Ans. B]
24. Which one among the following welding processes used non - consumable electrode?
 (A) Gas metal arc welding (C) Gas tungsten arc welding
 (B) Submerged arc welding (D) Flux coated arc welding
[Ans. C]
25. The crystal structure of austenite is
 (A) body centered cubic (C) hexagonal closed packed
 (B) face centered cubic (D) body centered tetragonal
[Ans. B]

Q. 26 - Q. 55 carry two marks each.

26. A torque T is applied at the free end of a stepped rod of circular cross-section as shown in the figure. The shear modulus of the material of the rod is G . the expression of d to produce an angular twist θ at the free end is



(A) $\left(\frac{32TL}{\pi\theta G}\right)^{\frac{1}{4}}$

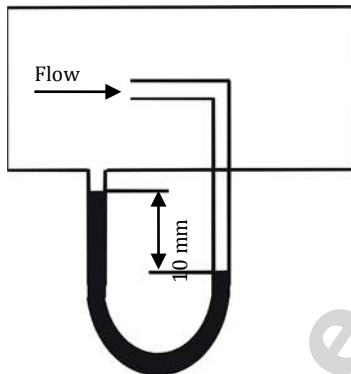
(C) $\left(\frac{16TL}{\pi\theta G}\right)^{\frac{1}{4}}$

(B) $\left(\frac{18TL}{\pi\theta G}\right)^{\frac{1}{4}}$

(D) $\left(\frac{2TL}{\pi\theta G}\right)^{\frac{1}{4}}$

[Ans. B]

27. Figure shows the schematic for the measurement of velocity of air (density = 1.2 kg/m^3) through a constant - area duct using a pitot tube and a water - tube manometer. The differential head of water (density = 1000 kg/m^3) in the two columns of the manometer is 10 mm. take acceleration due to gravity as 9.8 m/s^2 . The velocity of air in m/s is



(A) 6.4

(C) 12.8

(B) 9.0

(D) 25.6

[Ans. C]

28. The values of enthalpy of steam at the inlet and outlet of a steam turbine in a Rankine cycle are 2800 kJ/kg and 1800 kJ/kg respectively. Neglecting pump work, the specific steam consumption in kg/kW-hour is

(A) 3.60

(C) 0.06

(B) 0.36

(D) 0.01

[Ans. A]

29. The integral $\int_1^3 \frac{1}{x} dx$, when evaluated by using Simpson's 1/3 rule on two equal subintervals each of length 1, equals

(A) 1.000

(C) 1.111

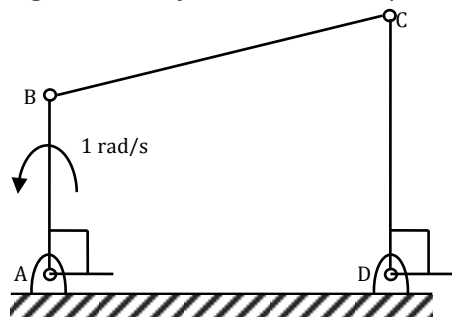
(B) 1.098

(D) 1.120

[Ans. C]

30. Two identical ball bearing P and Q are operating at loads 30 kN and 45 kN respectively. The ratio of the life of bearing P to the life of bearing Q is
- (A) 81/16 (C) 9/4
(B) 27/8 (D) 3/2
- [Ans. B]**

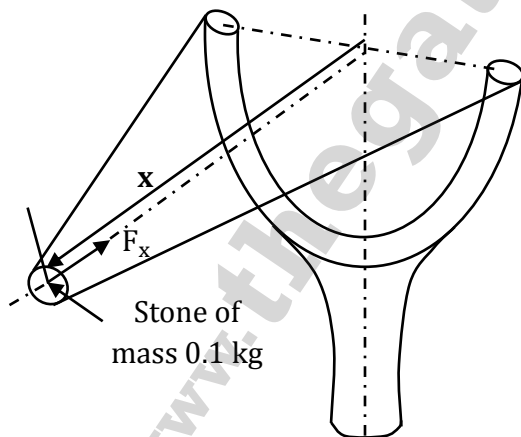
31. For the four-bar linkage shown in the figure, the angular velocity of link AB is 1 rad/s. The length of link CD is 1.5 times the length of link AB. In the configuration shown, the angular velocity of link CD in rad/s is



- (A) 3 (B) $\frac{3}{2}$ (C) 1 (D) $\frac{2}{3}$

[Ans. D]

32. A stone with mass of 0.1 kg is catapulted as shown in the figure. The total force F_x (in N) exerted by the rubber band as a function of distance x (in m) is given by $F_x = 300x^2$. If the stone is displaced by 0.1 m from the un-stretched position ($x = 0$) of the rubber band, the energy stored in the rubber band is



- (A) 0.01 J (C) 1 J
(B) 0.1 J (D) 10 J

[Ans. B]

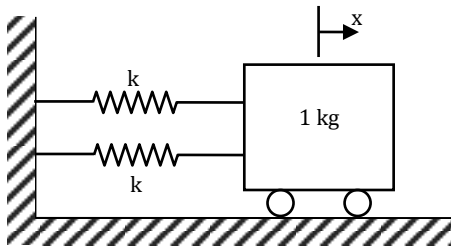
33. Consider the differential equation $\frac{dy}{dx} = (1 + y^2)x$. The general solution with constant c is

- (A) $y = \tan\left(\frac{x^2}{2} + \tan c\right)$ (C) $y = \tan^2\left(\frac{x}{2}\right) + c$
(B) $y = \tan^2\left(\frac{x}{2} + c\right)$ (D) $y = \tan\left(\frac{x^2}{2} + c\right)$

[Ans. D]

34. An unbiased coin is tossed five times. The outcome of each toss is either a head or a tail. The probability of getting at least one head is _____
- (A) $1/32$ (C) $16/32$
(B) $13/32$ (D) $31/32$
- [Ans. D]**

35. A mass of 1 kg is attached to two identical springs each with stiffness $k = 20 \text{ kN/m}$ as shown in the figure. Under frictionless condition, the natural frequency of the system in Hz is close to



- (A) 32 (C) 16
(B) 23 (D) 11
- [Ans. A]**

36. The shear strength of a sheet metal is 300MPa. The blanking force required to produce a blank of 100 mm diameter from a 1.5 mm thick sheet is close to
- (A) 45 kN (C) 141 kN
(B) 70 kN (D) 3500 kN
- [Ans. C]**

37. The ratios of the laminar hydrodynamic boundary layer thickness to thermal boundary layer thickness of flows of two fluids P and Q on a flat plate are $\frac{1}{2}$ and 2 respectively. The Reynolds numbers are based on the plate length for both flows is 10^4 . The Prandtl and Nusselt numbers for P are $1/8$ and 35 respectively. The prandtl and nusselt numbers for Q are respectively.
- (A) 8 and 140 (C) 4 and 70
(B) 8 and 70 (D) 4 and 35
- [Ans. A]**

38. The crank radius of a single – cylinder I. C. engine is 60 mm and the diameter of the cylinder is 80 mm. The swept volume of the cylinder in cm^3 is
- (A) 48 (C) 302
(B) 96 (D) 603
- [Ans. D]**

39. A pump handing a liquid raises its pressure form 1 bar to 30 bar. Take the density of the liquid as 990 kg/m^3 . The isentropic specific work done by the pump in kJ/kg is
- (A) 0.10 (C) 2.50
(B) 0.30 (D) 2.93
- [Ans. D]**

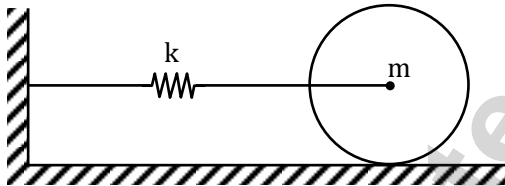
40. A spherical steel ball of 12 mm diameter at initially 1000 K. It is slowly cooled in surrounding 300 K. the heat transfer coefficient between steel ball and the surrounding is $5 \text{ W/m}^2\text{K}$. The thermal conductivity of steel is 20 W/mK . The temperature difference between center and the surface of steel ball is
- (A) Large because conduction resistance is far higher than the convective resistance.
 (B) Large because conduction resistance is far less than the convective resistance.
 (C) Small because conduction resistance is far higher than convective resistance.
 (D) Small because conduction resistance is far less than convective resistance.

[Ans. D]

41. An ideal Brayton cycle, operating between the pressure limits of 1 bar and 6 bar, has minimum and maximum temperatures of 300 K and 1500 K. The ratio of specific heats of the working fluid is 1.4. The approximate final temperatures in Kelvin at the end of the compression and expansion processes are respectively
- (A) 500 and 900 (C) 500 and 500
 (B) 900 and 500 (D) 900 and 900

[Ans. A]

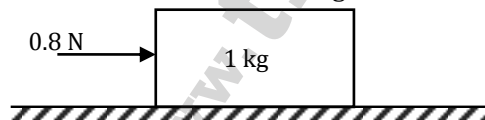
42. A disc of mass m is attached to a spring of stiff-ness k as shown in the fig. The disc rolls without slipping on a horizontal surface. The nature frequency of vibration of the system is



- (A) $\frac{1}{2\pi} \sqrt{\frac{k}{m}}$ (C) $\frac{1}{2\pi} \sqrt{\frac{2k}{3m}}$
 (B) $\frac{1}{2\pi} \sqrt{\frac{2k}{m}}$ (D) $\frac{1}{2\pi} \sqrt{\frac{3k}{2m}}$

[Ans. C]

43. A 1 kg block is resting on a surface with coefficient of friction $\mu = 0.1$. A force of 0.8 N is applied to the block as shown in the figure. The friction force is



- (A) 0 (B) 0.8 N (C) 0.98 N (D) 1.2N

[Ans. B]

44. Consider the following system of equations:

$$2x_1 + x_2 + x_3 = 0.$$

$$x_2 - x_3 = 0,$$

$$x_1 + x_2 = 0$$

The system has

- (A) A unique solution (C) Infinite number of solutions
 (B) No solution (D) Five solutions

[Ans. C]

45. A single – point cutting tool with 12° rake angle is used to machine a steel work – piece. The depth of cut, i.e. uncut thickness is 0.81 mm. The chip thickness under orthogonal machining condition is 1.8 mm. The shear angle is approximately
- (A) 22° (C) 56°
(B) 26° (D) 76°
- [Ans. B]**

46. Match the following non – traditional machining processes with the corresponding material removal mechanism:

Machining process

Mechanism of material removal

P. Chemical machining

1. Erosion

Q. Electro – chemical machining

2. Corrosive reaction

R. Electro discharge machining

3. Ion displacement

S. Ultrasonic machining

4. Fusion and vaporization

(A) P – 2, Q – 3, R – 4, S – 1

(C) P – 3, Q – 2, R – 4, S – 1

(B) P – 2, Q – 4, R – 3, S – 1

(D) P – 2, Q – 3, R – 1, S – 4

[Ans. A]

47. A cubic casting of 50 mm side undergoes volumetric solidification shrinkage and volumetric solid contraction of 4% and 6% respectively. No riser is used. Assume uniform cooling in all directions. The side of the cube after solidification and contraction is
- (A) 48.32 mm (C) 49.94 mm
(B) 49.90 mm (D) 49.96 mm
- [Ans. A]**

Common Data for Questions 48 and 49:

In an experimental set-up, airflows between two station P and Q adiabatically. The direction of flows depends on the pressure and temperature conditions maintained at P and Q. The condition at the P is 150 kPa and 350 K. The temperature at station Q is 300 K. The following are the properties and relations pertaining to air:

Specific heat at constant pressure, $C_p = 1.005$ kJ/kgK;

Specific heat at constant volume, $C_v = 0.718$ kJ/kgK;

Characteristic gas constant, $R = 0.287$ kJ/kgK

Enthalpy, $h = C_p T$

Internal energy, $u = C_v T$

48. If the air has to flow from station P to station Q, the maximum possible value of pressure in kPa at station Q is close to
- (A) 50 (C) 128
(B) 87 (D) 150
- [Ans. B]**

49. If the pressure at station Q is 50 kPa, the change in entropy ($S_Q - S_P$) in kJ/kgK is
- (A) -0.155 (C) 0.160
(B) 0 (D) 0.355
- [Ans. C]**

Common Data for Questions 50 and 51:

One unit of product P_1 requires 3 kg of resource R_1 and 1 kg of resource R_2 . One unit of product P_2 requires 2 kg of resource R_1 and 2 kg of resource R_2 . The profits per unit by selling product P_1 and P_2 are ₹ 2000 and ₹ 3000 respectively. The manufacturer has 90 kg of resource R_1 and 100 kg of resource R_2 .

50. The unit worth of resource R_2 i.e. dual price of resource R_2 in ₹ /kg is
 (A) 0 (C) 1500
 (B) 1350 (D) 2000

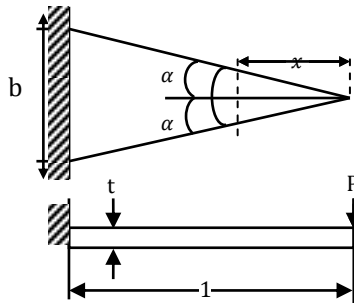
[Ans. A]

51. The manufacturer can make a maximum profit of ₹
 (A) 60000 (C) 150000
 (B) 135000 (D) 200000

[Ans. B]

Statement for Linked Answer Questions 52 and 53:

A triangular-shaped cantilever beam of uniform-thickness is shown in the figure. The young's modulus if the material of the beam is E . A concentrated load P is applied at the free end of the beam.



52. The maximum deflection of the beam is
 (A) $\frac{24Pl^3}{Ebt^3}$ (C) $\frac{8Pl^3}{Ebt^3}$
 (B) $\frac{12Pl^3}{Ebt^3}$ (D) $\frac{6Pl^3}{Ebt^3}$

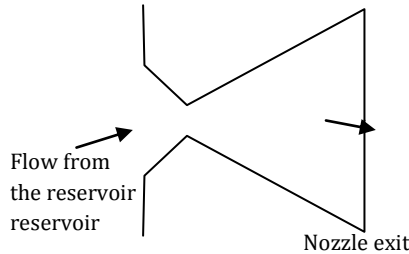
[Ans. D]

53. The area moment of inertia about the neutral axis of a cross-section at a distance x measure from the free end is
 (A) $\frac{bxt^3}{6l}$ (C) $\frac{bxt^3}{24l}$
 (B) $\frac{bxt^3}{12l}$ (D) $\frac{xt^3}{12}$

[Ans. B]

Statement for Linked Answer Questions 54 and 55:

The temperature and pressure of air in a large reservoir are 400k and 3 bar respectively. A converging-diverging nozzle of exit area 0.005m^2 is fitted to the wall of reservoir shown in figure. The static pressure of air at the exit section for isentropic flow through the nozzle is 50kPa. The characteristic gas constant and the ratio of specific heats of air are 0.287 kJ/kgK and 1.4 respectively.



54. The density of air in kg/m^3 at the nozzle exit is
 (A) 0.560 (C) 0.727
 (B) 0.600 (D) 0.800

[Ans. C]

55. The mass flow rate of air through the nozzle in kg/s is
 (A) 1.30 (C) 1.85
 (B) 1.77 (D) 2.06

[Ans. D]

General Aptitude (GA) Questions

Q. 56 – Q. 60 carry one mark each.

56. If $\text{Log}(P) = (1/2)\text{Log}(Q) = (1/3)\text{Log}(R)$, then which of the following options is TRUE?
 (A) $P^2 = Q^3R^2$ (C) $Q^2 = R^3P$
 (B) $Q^2 = PR$ (D) $R = P^2Q^2$

[Ans. B]

57. Which of the following options is the closest in the meaning to the word below:
 Inexplicable
 (A) Incomprehensible (C) Inextricable
 (B) Indelible (D) Infallible

[Ans. A]

58. Choose the word from the options given below that is most nearly opposite in meaning to the given word:
 Amalgamate
 (A) merge (C) collect
 (B) split (D) separate

[Ans. D]

59. Choose the most appropriate word from the options given below to complete the following sentence. If you are trying to make a strong impression on your audience, you cannot do so by being understated, tentative or
- (A) hyperbolic (C) argumentative
(B) restrained (D) indifferent

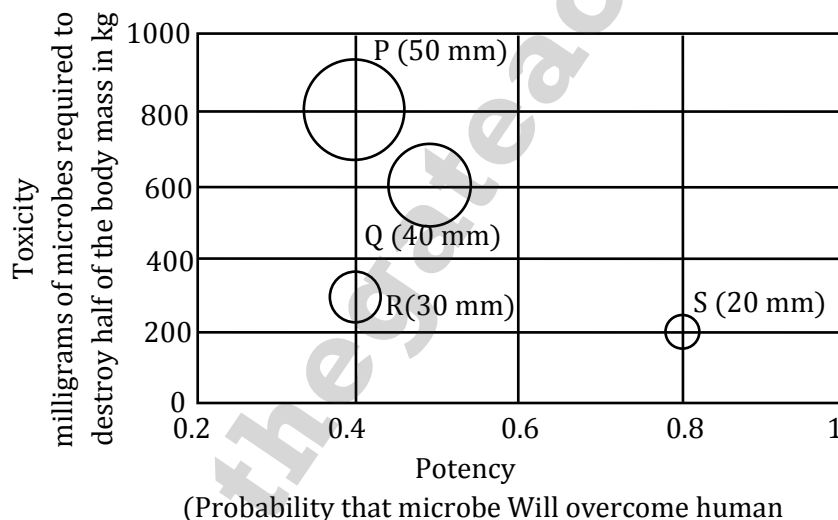
[Ans. B]

60. Choose the most appropriate word(s) from the options given below to complete the following sentence.
I contemplated Singapore for my vacation but decided against it.
- (A) to visit (C) visiting
(B) having to visit (D) for a visit

[Ans. C]

Q. 61 - Q. 65 carry two marks each.

61. P, Q, R and S are four types of dangerous microbes recently found in a human habitat. The area of each circle with its diameter printed in brackets represents the growth of a single microbe surviving human immunity system within 24 hours of entering the body. The danger to human beings varies proportionately with the toxicity, potency and growth attributed to a microbe shown in the figure



A pharmaceutical company is contemplating the development of a vaccine against the most dangerous microbe. Which microbe should the company target in its first attempt?

- (A) P (B) Q (C) R (D) S

[Ans. A]

62. Few school curricula include a unit on how to deal with bereavement and grief, and yet all the students at some point in their lives suffer from losses through death and parting. Based on the above passage which topic would not be included in a unit on bereavement?
- (A) How to write a letter of condolence
(B) What emotional stages are passed through in the healing process
(C) What the leading causes of death are
(D) How to give support to a grieving friend

[Ans. C]

63. A container originally contains 10 litres of pure spirit. From this container 1 litre of spirit is replaced with 1 litre of water. Subsequently, 1 litre of the mixture is again replaced with 1 litre of water and this process is repeated one more time. How much spirit is now left in the container?
- (A) 7.58 litres (C) 7 litres
(B) 7.84 litres (D) 7.29 litres
- [Ans. D]**
64. A transporter receives the same number of orders each day. Currently, he has some pending orders (backlog) to be shipped. If he uses 7 trucks, then at the end of the 4th day he can clear all the order. Alternatively, if he uses only 3 trucks, then all the orders are cleared at the end of the 10th day. What is the minimum number of trucks required so that there will be no pending order at the end of the 5th day?
- (A) 4 (C) 6
(B) 5 (D) 7
- [Ans. C]**
65. The variable cost (V) of manufacturing a product varies according to the equation $V = 4q$, where q is the quantity produced. The fixed cost (F) of production of same product reduces with q according to the equation $F = 100/q$. How many units should be produced to minimize the total cost (V+F)?
- (A) 5 (C) 7
(B) 4 (D) 6
- [Ans. B]**