GATE-2011

Question Paper
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## GATE-2011- ECE

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GATE 2011 Examination
Electronics and Communication Engineering

Q.1 - Q.25 Carry One Mark each.

1. The modes in a rectangular waveguide are denoted by TE_{mn}/TM_{mn} where \( m \) and \( n \) are the Eigen numbers along the larger and smaller dimensions of the waveguide respectively. Which one of the following statements is TRUE?
   (A) The TM_{10} mode of the waveguide does not exist
   (B) The TE_{10} mode of the waveguide does not exist
   (C) The TM_{10} and the TE_{10} modes both exist and have the same cut off frequencies
   (D) The TM_{10} and the TM_{01} modes both exist and have the same cut off frequencies

   [Ans. A]

2. The list-I the attributes and the list-II the modulation system. Match the attribute to the modulation system that best meets it.

   List-I
   P. Power efficient transmission signals
   Q. Most bandwidth efficient transmission of voice signals
   R. Simplest receiver structure
   S. Bandwidth efficient transmission of signals with significant dc component

   List-II
   i. Conventional AM
   ii. FM
   iii. VSB
   iv. SSB-SC

   Codes:
   (A) P-iv, Q-ii, R-i, S-iii
   (B) P-ii, Q-iv, R-i, S-iii
   (C) P-iii, Q-ii, R-i, S-iv
   (D) P-ii, Q-iv, R-iii, S-i

   [Ans. B]

3. The differential equation
   \[ 100 \frac{d^2y}{dt^2} - 20 \frac{dy}{dt} + y = x(t) \]
   describes a system with an input \( x(t) \) and an output \( y(t) \). The system, which is initially relaxed, is excited by a unit step input. The output \( y(t) \) can be represented by the waveform

   (A) \hspace{1cm} (B)

   [Diagram showing two different waveforms for y(t) over time]
4. For the transfer function
   \[ G(j\omega) = 5 + j\omega \], the corresponding Nyquist plot for the positive frequency has the form
   (A)
   \[ \text{(B)} \]
   \[ \text{(C)} \]
   \[ \text{(D)} \]

   \[ \text{[Ans. A]} \]

5. The trigonometric Fourier series of an even function does not have the
   (A) Dc term
   (B) Cosine terms
   (C) Sine terms
   (D) Odd harmonic terms

   \[ \text{[Ans. C]} \]

6. When the output Y in the circuit below is “1”, it implies that data has
   \[ \text{(A)} \text{ Changed from } “0” \text{ to } “1” \]
   \[ \text{(B)} \text{ Changed from } “1” \text{ to } “0” \]
   \[ \text{(C)} \text{ Changed in either direction} \]
   \[ \text{(D)} \text{ Not changed} \]

   \[ \text{[Ans. A]} \]
7. The logic function implemented by the circuit below is (ground implies a logic "0")

\[ F = \text{XOR}(P, Q) \]

[Ans. D]

8. The circuit below implements a filter between the input current \( i_i \) and the output voltage \( v_o \). Assume that the opamp is ideal. The filter implemented is a

\[ \text{(B) band pass filter} \]

[Ans. D]

9. A silicon PN junction is forward biased with a constant current at room temperature. When the temperature is increased by 10°C, the forward bias voltage across the PN junction

\[ \text{(D) Decreases by 25 mV} \]

[Ans. D]

10. In the circuit shown below, the Norton equivalent current in amperes with respect to the terminals P and Q is

\[ \text{(A) } 6.4 - j4.8 \]

[Ans. A]
11. In the circuit shown below, the value of \( R_L \) such that the power transferred to \( R_L \) is maximum is

\[
\begin{align*}
\text{(A)} & \ 5\Omega \\
\text{(B)} & \ 10\Omega \\
\text{(C)} & \ 15\Omega \\
\text{(D)} & \ 20\Omega
\end{align*}
\]

[Ans. C]

12. The value of the integral \( \oint \frac{\mathrm{e}^{-3z+4}}{z^2+4z+5} \, \mathrm{d}z \) where \( c \) is the circle \( |z| = 1 \) is given by

\[
\begin{align*}
\text{(A)} & \ 0 \\
\text{(B)} & \ 1/10 \\
\text{(C)} & \ 4/5 \\
\text{(D)} & \ 1
\end{align*}
\]

[Ans. A]

13. A transmission line of characteristic impedance 50 \( \Omega \) is terminated by a 50 \( \Omega \) load. When excited by a sinusoidal voltage source at 10 GHz, the phase difference between two points spaced 2 mm apart on the line is found to be \( \pi/4 \) radians. The phase velocity of the wave along the line is

\[
\begin{align*}
\text{(A)} & \ 0.8 \times 10^8 \text{ m/s} \\
\text{(B)} & \ 1.2 \times 10^8 \text{ m/s} \\
\text{(C)} & \ 1.6 \times 10^8 \text{ m/s} \\
\text{(D)} & \ 3 \times 10^8 \text{ m/s}
\end{align*}
\]

[Ans. C]

14. Consider the following statements regarding the complex Poynting vector \( \vec{S} \) for the power radiated by a point source in an infinite homogeneous and lossless medium \( \text{Re}(\vec{S}) \) denotes the real part of \( \vec{S} \), \( S \) denotes a spherical surface whose centre is at the point source, and \( \hat{n} \) denotes the unit surface normal on \( S \). Which of the following statements is TRUE?

\[
\begin{align*}
\text{(A)} & \ \text{Re}(\vec{S}) \text{ remains constant at any radial distance for the source} \\
\text{(B)} & \ \text{Re}(\vec{S}) \text{ increases with increasing radial distance from the source} \\
\text{(C)} & \ \oint_S \text{Re}(\vec{S}) \cdot \hat{n} \, \mathrm{d}S \text{ remains constant at any radial distance from the source} \\
\text{(D)} & \ \oint_S \text{Re}(\vec{S}) \cdot \hat{n} \, \mathrm{d}S \text{ decreases with increasing radial distance from the source}
\end{align*}
\]

[Ans. C]

15. An analog signal is band-limited to 4 KHz. Sampled at the Nyquist rate and the samples are quantized into 4 levels. The quantized levels are assumed to be independent and equally probable. If we transmit two quantized samples per second, the information rate is

\[
\begin{align*}
\text{(A)} & \ 1 \text{ bit/sec} \\
\text{(B)} & \ 2 \text{ bits/sec} \\
\text{(C)} & \ 3 \text{ bits/sec} \\
\text{(D)} & \ 4 \text{ bits/sec}
\end{align*}
\]

[Ans. D]
16. The root locus plot for a system is given below. The open loop transfer function corresponding to this plot is given by

\[ G(s)H(s) = k \frac{s(s + 1)}{(s + 2)(s + 3)} \]

(A) \[ G(s)H(s) = k \frac{s(s + 1)}{(s + 2)(s + 3)} \]
(B) \[ G(s)H(s) = k \frac{(s + 1)}{s(s + 2)(s + 3)^2} \]
(C) \[ G(s)H(s) = k \frac{1}{(s + 1)(s + 2)(s + 3)} \]
(D) \[ G(s)H(s) = k \frac{(s + 1)}{s(s + 2)s + 3)} \]

[Ans. B]

17. A system is defined by its impulse response \( h(n) = 2^n u(n - 2) \). The system is
(A) Stable and causal
(B) Causal but not stable
(C) Stable but not causal
(D) Unstable and non-causal

[Ans. B]

18. If the unit step response of a network is \( (1 - e^{-at}) \), then its unit impulse response is
(A) \( \alpha e^{-at} \)
(B) \( \alpha^{-1} e^{-at} \)
(C) \( (1 - \alpha^{-1}) e^{-at} \)
(D) \( (1 - \alpha) e^{-at} \)

[Ans. A]

19. The output \( Y \) in the circuit below is always “1” when

(A) Two or more of the inputs \( P, Q, R \) are “0”
(B) Two or more of the inputs \( P, Q, R \) are “1”
(C) Any odd number of the inputs \( P, Q, R \) is “0”
(D) Any odd number of the inputs \( P, Q, R \) is “1”

[Ans. B]

20. In the circuit shown below, capacitors \( C_1 \) and \( C_2 \) are very large and are shorts at the input frequency. \( v_i \) is a small signal input. The gain magnitude \( |v_o/v_i| \) at 10 Mrad/s is
21. Drift current in semiconductors depends upon
(A) Only the electric field
(B) Only the carrier concentration gradient
(C) Both the electric field and the carrier concentration
(D) Both the electric field and the carrier concentration gradient
[Ans. C]

22. A Zener diode, when used in voltage stabilization circuits, is biased in
(A) reverse bias region below the breakdown voltage
(B) reverse breakdown region
(C) forward bias region
(D) forward bias constant current mode
[Ans. B]

23. The circuit shown below is driven by a sinusoidal input \( v_i = V_p \cos(t/RC) \). The steady state output \( v_o \) is

(A) \( (V_p/3) \cos(t/RC) \)
(B) \( (V_p/3) \sin(t/RC) \)
(C) \( (V_p/2) \cos(t/RC) \)
(D) \( (V_p/2) \sin(t/RC) \)
[Ans. A]
24. Consider a closed surface \( S \) surrounding a volume \( V \). If \( \vec{r} \) is the position vector of a point inside \( S \), with \( \vec{n} \) the unit normal on \( S \), the value of the integral \( \oint \vec{r} \cdot \vec{n} \, dS \) is

(A) 3V  
(B) 5V  
(C) 10V  
(D) 15V

[Ans. D]

25. The solution of the differential equation \( \frac{dy}{dx} = ky \), \( y(0) = c \) is

(A) \( x = ce^{-ky} \)  
(B) \( x = ke^{xy} \)  
(C) \( y = ce^{ky} \)  
(D) \( y = ce^{-ky} \)

[Ans. C]

Q.26 - Q.55 Carry Two Mark each.

26. The electric and magnetic fields for a TEM wave of frequency 14 GHz in a homogeneous medium of relative permittivity \( \varepsilon_r \) and relative permeability \( \mu_r = 1 \) are given by

\[
\vec{E} = E_p e^{i(\omega t - 2\pi ft)} \hat{z} \text{ V/m}
\]
\[
\vec{H} = 3E_p e^{i(\omega t - 2\pi ft)} \hat{x} \text{ A/m}
\]

Assuming the speed of light in free space to be \( 3 \times 10^8 \text{ m/s} \), the intrinsic impedance of free space to be \( 120\pi \), the relative permittivity \( \varepsilon_r \) of the medium and the electric field amplitude \( E_p \) are

(A) \( \varepsilon_r = 3, E_p = 120\pi \)  
(B) \( \varepsilon_r = 3, E_p = 360\pi \)  
(C) \( \varepsilon_r = 9, E_p = 360\pi \)  
(D) \( \varepsilon_r = 9, E_p = 120\pi \)

[Ans. D]

27. A message signal \( m(t) = \cos 2000\pi t + 4 \cos 4000\pi t \) modulates the carrier \( c(t) = \cos 2\pi f_c t \), where \( f_c = 1 \text{ MHz} \) to produce an AM signal. For demodulating the generated AM signal using an envelope detector, the time constant \( RC \) of the detector circuit should satisfy.

(A) \( 0.5 \text{ ms} < RC < 1 \text{ ms} \)  
(B) \( 1 \mu s < RC < 0.5 \text{ ms} \)  
(C) \( RC \ll 1 \mu s \)  
(D) \( RC \gg 0.5 \text{ ms} \)

[Ans. B]

28. The block diagram of a system with one input \( u \) and two outputs \( y_1 \) and \( y_2 \) is given below.

\[
\begin{array}{c}
\text{Input} \quad u \\
\downarrow \\
\frac{1}{s+2} \\
\downarrow \\
y_1 \\
\downarrow \\
\frac{2}{s+2} \\
\downarrow \\
y_2
\end{array}
\]

A state space model of the above system in terms of the state vector \( \vec{x} \) and the output vector \( \vec{y} = [y_1 \ y_2]^T \) is

(A) \( \dot{\vec{x}} = [2] \vec{x} + [1] u; \quad \vec{y} = [1 \ 2] \vec{x} \)

(B) \( \dot{\vec{x}} = [-2] \vec{x} + [1] u; \quad \vec{y} = [1 \ 2] \vec{x} \)

(C) \( \dot{\vec{x}} = \begin{bmatrix} 0 & 1 \\ -2 & 0 \end{bmatrix} \vec{x} + [1] u; \quad \vec{y} = [1 \ 2] \vec{x} \)

(D) \( \dot{\vec{x}} = \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix} \vec{x} + [1] u; \quad \vec{y} = [1 \ 2] \vec{x} \)

[Ans. B]
29. Two systems \( H_1(z) \) and \( H_2(z) \) are connected in cascade as shown below. The overall output \( y(n) \) is the same as the input \( x(n) \) with a one unit delay. The transfer function of the second system \( H_2(z) \) is

\[
\begin{align*}
H_1(z) &= \frac{(1 - 0.4z^{-1})}{(1 - 0.6z^{-1})} \\
H_2(z) &= \frac{1}{z^{-1}(1 - 0.4z^{-1})} \\
\end{align*}
\]

(A) \( \frac{(1 - 0.6z^{-1})}{z^{-1}(1 - 0.4z^{-1})} \) \\
(B) \( \frac{(1 - 0.4z^{-1})}{(1 - 0.6z^{-1})} \) \\
(C) \( \frac{z^{-1}(1 - 0.4z^{-1})}{(1 - 0.6z^{-1})} \) \\
(D) \( \frac{z^{-1}(1 - 0.4z^{-1})}{(1 - 0.6z^{-1})} \) \\

[Ans. B]

30. An 8085 assembly language program is given below. Assume that the carry flag is initially unset. The content of the accumulator after the execution of the program is

\[
\begin{align*}
\text{MVI A, 07H} \\
\text{RLC} \\
\text{MOV B, A} \\
\text{RLC} \\
\text{RLC} \\
\text{ADD B} \\
\text{RRC} \\
\end{align*}
\]

(A) 8CH \\
(B) 64H \\
(C) 23H \\
(D) 15H \\

[Ans. C]

31. The first six points of the 8-point DFT of a real valued sequence are 5, \( 1-j3 \), 0, \( 3-j4 \), 0 and \( 3+j4 \). The last two points of the DFT are respectively

(A) 0, \( 1-j3 \) \\
(B) 0, \( 1+j3 \) \\
(C) \( 1-j3 \), \( 5 \) \\
(D) \( 1+j3 \), \( 5 \) \\

[Ans. B]

32. For the BJT \( Q_1 \) in the circuit shown below, \( \beta = \infty \), \( V_{BE_{on}} = 0.7V \), \( V_{CE_{sat}} = 0.7V \). The switch is initially closed. At time \( t = 0 \), the switch is opened. The time \( t \) at which \( Q_1 \) leaves the active region is

(A) 10 ms \\
(B) 25 ms \\
(C) 50 ms \\
(D) 100 ms \\

[Ans. B]
33. In the circuit shown below, the network $N$ is described by the following $Y$ matrix:

$$Y = \begin{bmatrix} 0.1 \, \text{S} & -0.01 \, \text{S} \\ 0.01 \, \text{S} & 0.1 \, \text{S} \end{bmatrix}$$

The voltage gain $\frac{V_2}{V_1}$ is

(A) $\frac{1}{90}$  
(B) $\frac{-1}{90}$  
(C) $\frac{-1}{99}$  
(D) $\frac{-1}{11}$

[Ans. D]

34. In the circuit shown below, the initial charge on the capacitor is 2.5 mC, with the voltage polarity as indicated. The switch is closed at time $t = 0$. The current $i(t)$ at a time $t$ after the switch is closed is

$$100 \, \text{V}$$

(A) $i(t) = 15 \exp(-2 \times 10^3 t) \, \text{A}$  
(B) $i(t) = 5 \exp(-2 \times 10^3 t) \, \text{A}$  
(C) $i(t) = 10 \exp(-2 \times 10^3 t) \, \text{A}$  
(D) $i(t) = -5 \exp(-2 \times 10^3 t) \, \text{A}$

[Ans. A]

35. The system of equations

$$\begin{align*}
    x + y + z &= 6 \\
    x + 4y + 6z &= 20 \\
    x + 4y + \lambda z &= \mu
\end{align*}$$

has NO solution for values of $\lambda$ and $\mu$ given by

(A) $\lambda = 6, \mu = 20$  
(B) $\lambda = 6, \mu \neq 20$  
(C) $\lambda \neq 6, \mu = 20$  
(D) $\lambda \neq 6, \mu \neq 20$

[Ans. B]

36. A fair dice is tossed two times. The probability that the second toss results in a value that is higher than the first toss is

(A) $\frac{2}{36}$  
(B) $\frac{2}{6}$  
(C) $\frac{5}{12}$  
(D) $\frac{1}{2}$

[Ans. C]

37. A current sheet $\mathbf{J} = 10\hat{u}_y \, \text{A/m}$ lies on the dielectric interface $x = 0$ between two dielectric media with $\varepsilon_{r1} = 5, \mu_{r1} = 1$ in Region $-1$ ($x < 0$) and $\varepsilon_{r2} = 2, \mu_{r2} = 2$ in Region $-2$ ($x > 0$). If the magnetic field in Region $-1$ at $x = 0^-$ is
\[ \mathbf{H}_1 = 3\hat{u}_x + 30\hat{u}_y \text{ A/m}, \text{the magnetic field in Region } -2 \text{ at } x = 0^+ \text{ is} \]

- (A) \[ \mathbf{H}_2 = 1.5\hat{u}_x + 30\hat{u}_y - 10\hat{u}_z \text{ A/m} \]
- (B) \[ \mathbf{H}_2 = 3\hat{u}_x + 30\hat{u}_y - 10\hat{u}_z \text{ A/m} \]
- (C) \[ \mathbf{H}_2 = 1.5\hat{u}_x + 40\hat{u}_y \text{ A/m} \]
- (D) \[ \mathbf{H}_2 = 3\hat{u}_x + 30\hat{u}_y + 10\hat{u}_z \text{ A/m} \]

[Ans. A]

38. A transmission line of characteristic impedance 50 \( \Omega \) is terminated in a load impedance \( Z_L \). The VSWR of the line is measured as 5 and the first of the voltage maxima in the line is observed at a distance of \( \lambda/4 \) from the load. The value of \( Z_L \) is

- (A) \( 10 \) \( \Omega \)
- (B) \( 250 \) \( \Omega \)
- (C) \( (19.23 + j46.15) \) \( \Omega \)
- (D) \( (19.23 - j46.15) \) \( \Omega \)

[Ans. A]

39. \( X(t) \) is a stationary random process with autocorrelation function \( R_X(\tau) = \exp(-\pi \tau^2) \). This process passed through the system shown below. The power spectral density of the output process \( Y(t) \) is

- (A) \( (4\pi^2f^2 + 1) \exp(-\pi f^2) \)
- (B) \( (4\pi^2f^2 - 1) \exp(-\pi f^2) \)
- (C) \( (4\pi^2f^2 + 1) \exp(-\pi f) \)
- (D) \( (4\pi^2f^2 - 1) \exp(-\pi f) \)

[Ans. A]

40. The output of a 3-stage Johnson (twisted-ring) counter is fed to a digital-to-analog (D/A) converter as shown in the figure below. Assume all states of the counter to be unset initially. The waveform which represents the D/A converter output \( V_0 \) is

- (A)
- (B)
41. Two D flip-flops are connected as a synchronous counter that goes through the following sequence: \( Q_B Q_A = 00 \rightarrow 11 \rightarrow 01 \rightarrow 10 \rightarrow 00 \rightarrow \cdots \) The connections to the inputs \( D_A \) and \( D_B \) are:

(A) \( D_A = Q_B, D_B = Q_A \)
(B) \( D_A = \overline{Q}_B, D_B = \overline{Q}_A \)
(C) \( D_A = (Q_A \overline{Q}_B + \overline{Q}_A Q_B), D_B = Q_A \)
(D) \( D_A = (Q_A Q_B + \overline{Q}_A \overline{Q}_B), D_B = \overline{Q}_B \)

[Ans. D]

42. In the circuit shown below, for the MOS transistor, \( \mu_n C_{ox} = 100 \mu A/V^2 \) and the threshold voltage \( V_T = 1V \). The voltage \( V_s \) at the source of the upper transistor is:

(A) 1 V
(B) 2 V
(C) 3 V
(D) 3.67 V

[Ans. C]

43. An input \( x(t) = \exp(-2t)u(t) + \delta(t - 6) \) is applied to an LTI system with impulse response \( h(t) = u(t) \). The output is:

(A) \( [1 - \exp(-2t)]u(t) + u(t + 6) \)
(B) \( [1 - \exp(-2t)]u(t) + u(t - 6) \)
(C) \( 0.5[1 - \exp(-2t)]u(t) + u(t + 6) \)
(D) \( 0.5[1 - \exp(-2t)]u(t) + u(t - 6) \)

[Ans. D]

44. For a BJT, the common-base current gain \( \alpha = 0.98 \) and the collector base junction reverse bias saturation current \( I_{CO} = 0.6 \mu A \). This BJT is connected in the common emitter mode and operated in the active region with a base drive current \( I_B = 20 \mu A \). The collector current \( I_C \) for this mode of operation is:

(A) 0.98 mA
(B) 0.99 mA
(C) 1.0 mA
(D) 1.01 mA

[Ans. D]
45. If \( F(s) = L[f(t)] = \frac{2(s+1)}{s^2+4s+7} \) then the initial and final values of \( f(t) \) are respectively
   (A) 0, 2  
   (B) 2, 0  
   (C) 0, 2/7  
   (D) 2/7, 0  
   [Ans. B]

46. In the circuit shown below, the current \( I \) is equal to
   ![Circuit Diagram]
   (A) 1.4 \( \angle 0^\circ \) A  
   (B) 2.0 \( \angle 0^\circ \) A  
   (C) 2.8 \( \angle 0^\circ \) A  
   (D) 3.2 \( \angle 0^\circ \) A  
   [Ans. B]

47. A numerical solution of the equation \( f(x) = x + \sqrt{x} - 3 = 0 \) can be obtained using Newton–Raphson method. If the starting value is \( x_0 = 2 \) for the iteration, the value of \( x \) that is to be used in the next step is
   (A) 0.306  
   (B) 0.739  
   (C) 1.694  
   (D) 2.306  
   [Ans. C]

**Common Data for Q. No 48 and 49**

The channel resistance of an N-channel JFET shown in the figure below is 600 \( \Omega \) when the full channel thickness (\( t_{ch} \)) of 10 \( \mu m \) is available for conduction. The built-in voltage of the gate P+N junction (\( V_{bi} \)) is -1V. When the gate to source voltage (\( V_{GS} \)) is 0 V, the channel is depleted by 1 \( \mu m \) on each side due to the built-in voltage and hence the thickness available for conduction is only 8 \( \mu m \)

![JFET Diagram]

48. The channel resistance when \( V_{GS} = 0 \) V is
   (A) 480 \( \Omega \)  
   (B) 600 \( \Omega \)  
   (C) 750 \( \Omega \)  
   (D) 1000 \( \Omega \)  
   [Ans. C]
49. The channel resistance when $V_{GS} = -3 \, V$ is
   (A) 360 $\Omega$  
   (B) 917 $\Omega$  
   (C) 1000 $\Omega$  
   (D) 3000 $\Omega$  
   [Ans. C]

**Common Data for Q.No 50 and 51**

The input – output transfer function of a plant $H(s) = \frac{100}{s(s+10)^2}$ The plant is placed in a unity negative feedback configuration as shown in the figure below.

50. The signal flow graph that DOES NOT model the plant transfer function $H(s)$ is
   (A)  
   (B)  
   (C)  
   (D)  
   [Ans. D]

51. The gain margin of the system under closed loop unity negative feedback is
   (A) 0 dB  
   (B) 20 dB  
   (C) 26 dB  
   (D) 46 dB  
   [Ans. C]

**Statement for Linked Question 52 and 53**

A four-phase and an eight-phase signal constellation are show in the figure below.

52. For the constraint that the minimum distance between pairs of signal points be $d$ for both constellations, the radii $r_1$ and $r_2$ of the circles are
   (A) $r_1 = 0.707d, r_2 = 2.782d$  
   (B) $r_1 = 0.707d, r_2 = 1.932d$  
   (C) $r_1 = 0.707d, r_2 = 1.545d$  
   (D) $r_1 = 0.707d, r_2 = 1.307d$  
   [Ans. D]
53. Assuming high SNR and that all signals are equally probable, the additional average transmitted signal energy required by the 8-PSK signal to achieve the same error probability as the 4-PSK signal is
   (A) 11.90 dB
   (B) 8.73 dB
   (C) 6.79 dB
   (D) 5.33 dB
   [Ans. D]

Statements for Linked Answer Q. No 54 & 55

In the circuit shown below, assume that the voltage drop across a forward biased diode is 0.7V. The thermal voltage $V_t = kT/q = 25mV$. The small signal input $v_i = V_p \cos(\omega t)$ where $V_p = 100$ mV.

54. The bias current $I_{DC}$ through the diodes is
   (A) 1 mA
   (B) 1.28 mA
   (C) 1.5 mA
   (D) 2 mA
   [Ans. A]

55. The ac output voltage $v_{ac}$ is
   (A) 0.25 cos(\omega t) mV
   (B) 1 cos(\omega t) mV
   (C) 2 cos(\omega t) mV
   (D) 22 cos(\omega t) mV
   [Ans. B]

General Aptitude One Marks Question Q. 56 to Q. 60

56. The question below consists of a pair of related words followed by four pairs of words. Select the pair that best expresses the relation in the original pair:
   Gladiator: Arena
   (A) dancer: stage  
   (B) commuter: train  
   (C) teacher: classroom  
   (D) lawyer: courtroom
   [Ans. D]

57. There are two candidates P and Q in an election. During the campaign, 40% of the voters promised to vote for P, and rest for Q. However, on the day of election 15% of the voters went back on their promise to vote for P and instead voted for Q. 25% of the voters went back on their promise to vote for Q and instead voted for P. Suppose, P lost by 2 votes, then what was the total number of voters?
   (A) 100  
   (B) 110  
   (C) 90  
   (D) 95
   [Ans. A]
58. Choose the most appropriate word from the options given below to complete the following sentence:
It was her view that the country's problems had been by foreign technocrats, so that to invite them to come back would be counter-productive.
(A) Identified
(B) Ascertained
(C) Texacerbated
(D) Analysed
[Ans. C]

59. Choose the word from the options given below that is most nearly opposite in meaning to the given word:
Frequency
(A) periodicity
(B) rarity
(C) gradualness
(D) persistency
[Ans. B]

60. Choose the most appropriate word from the options given below to complete the following sentence: Under ethical guidelines recently adopted by the Indian Medical Association, human genes are to be manipulated only to correct diseases for which unsatisfactory.
(A) Similar
(B) Most
(C) Uncommo
(D) Available
[Ans. D]

61. The horse has played a little known but very important role in the field of medicine. Horses were injected with toxins of diseases until their blood built up immunities. Then a serum was made from their blood. Serums to fight with diphtheria and tetanus were developed this way. It can be inferred from the passage that horses were
(A) given immunity to diseases
(B) generally quite immune to diseases
(C) given medicines to fight toxins
(D) given diphtheria and tetanus serums
[Ans. B]

62. The fuel consumed by a motorcycle during a journey while travelling at various speeds is indicated in the graph below.

The distances covered during four laps of the journey are listed in the table below.
### 63. Fuel Consumption Analysis

<table>
<thead>
<tr>
<th>Lap</th>
<th>Distance (kilometers)</th>
<th>Average Speed (km/h)</th>
</tr>
</thead>
<tbody>
<tr>
<td>P</td>
<td>15</td>
<td>15</td>
</tr>
<tr>
<td>Q</td>
<td>75</td>
<td>45</td>
</tr>
<tr>
<td>R</td>
<td>40</td>
<td>75</td>
</tr>
<tr>
<td>S</td>
<td>10</td>
<td>10</td>
</tr>
</tbody>
</table>

From the given data we can conclude that the fuel consumed per kilometer was least during the lap

(A) P  
(B) Q  
(C) R  
(D) S

[Ans. A]

### 64. Toffee Sharing Problem

Three friends, R, S and T shared toffee from a bowl. R took \(\frac{1}{3}\)rd of the toffees, but returned four to the bowl. S took \(\frac{1}{4}\)th of what was left but returned three toffees to the bowl. T took half of the remainder but returned two back into the bowl. If the bowl had 17 toffees left, how many toffees were originally there in the bowl?

(A) 38  
(B) 31  
(C) 48  
(D) 41

[Ans. C]

### 65. Sum of Series

The sum of \(n\) terms of the series \(4 + 44 + 444 + \cdots\) is

(A) \(\left(\frac{4}{81}\right)[10^{n+1} - 9n - 1]\)  
(B) \(\left(\frac{4}{81}\right)[10^{n-1} - 9n - 1]\)  
(C) \(\left(\frac{4}{81}\right)[10^{n+1} - 9n - 10]\)  
(D) \(\left(\frac{4}{81}\right)[10^n - 9n - 10]\)

[Ans. C]